

# Sila a zrýchlenie

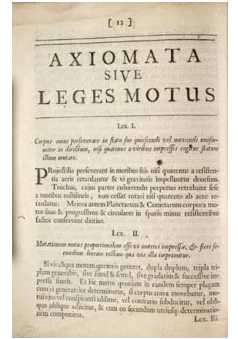
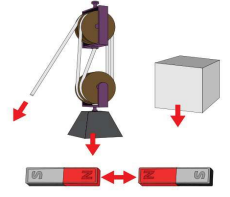
Richard Balogh: Sila a zrýchlenie.  
MEMS Inteligentné senzory a aktuátory, 11. 4. 2023

## Sila

slov. od 14. stor., úsilie

- LAT vis (*vis major*, strength, force, power)
- GB force (lat. fortis -> fr. force -> en. force)
- DE Kraft
- FR force
- PL siła
- HU erő
- UA сила [sila]
- RU сила [sila]
- CZ síla

Isaac Newton: *Principia Mathematica*, 1687.  
[https://la.wikipedia.org/wiki/Leges\\_motus\\_Newtoni](https://la.wikipedia.org/wiki/Leges_motus_Newtoni)



## Sila

- Sila je fyzikálna veličina, ktorá predstavuje veľkosť vzájomného pôsobenia telies.
  - Značka **F** / jednotka Newton [N]
  - 1 newton je sila, ktorá udelí telesu s hmotnosťou 1 kg zrýchlenie jeden meter za sekundu na druhú.
  - $1N = kg \cdot m \cdot s^{-2}$
2. Newtonov zákon  $F = m \cdot a$

Presná definícia (aj vzhľadom na to, že je to jedna zo základných veličín) nie je jednoduchá.  
Na makroskopickú úroveň môžeme vzájomné pôsobenie telies (ktoré pozorujeme na základe našej skúsenosti) našťastie opísať jedinou a jednoduchou vektorovou veličinou.

## 9.3. Snímače sily

- 
- 
- deformačné členy + snímanie :
  - mech. napätia - tenzometre
  - zmeny polohy - malé výchylky [mm, um]
- piezoelektrické - nevhodné pre statické merania
- kapacitné
- magnetoanizotropné
- zmena elektrického odporu

## 9.3. Snímače sily - aplikácie

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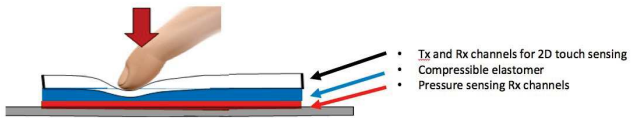
	<b>ALF304 Brake Pedal Force Sensor</b> Compact, low profile loadcell for measuring brake pedal application forces	Measurement Range 2.5kN	Accuracy [%] ±0.05% of F.S.	Output mV/V	Load direction Compression
	<b>ALF305 Seat Belt Tension Force Sensor</b> High performance loadcell for measuring seat belt tension forces	Measurement Range 16kN	Accuracy [%] ±3% of F.S.	Output mV/V	Load direction Tension
	<b>ALF319 Hand Brake Force Sensor</b> An excellent technical solution to measurement of an ergonomic force	Measurement Range 1kN	Accuracy [%] ±0.05% of F.S.	Output mV/V	Load direction Compression
	<b>ALF321 Gear Shift Force Sensor</b> Measures gear lever forces required to achieve gear selection	Measurement Range 200N	Accuracy [%] ±0.5% of F.S.	Output mV/V	Load direction Bi-directional

## 9.3. Snímače sily - aplikácie

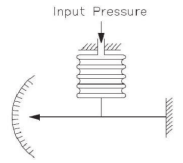
Force-sensing: A third dimension in automotive touch controls



Synaptics demonstration of a steering wheel touchpad with force sensing and haptics.

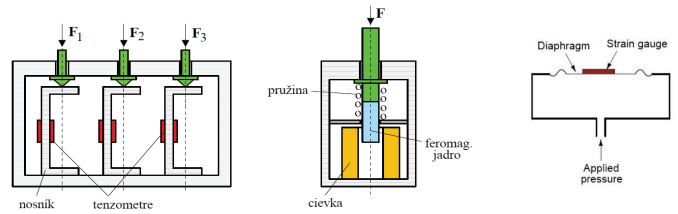


## 9.3. Snímače sily Deformačné členy

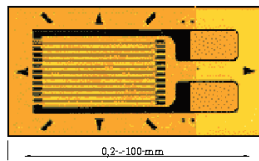


Menia pôsobiacu silu na inú veličinu

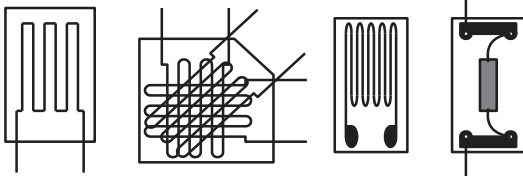
- **nosníky** → deformácia, tenzometre
- **pružiny** → zmena polohy, snímač polohy (indukčný, fotoelektrický)
- **pružné podložky** → zmena polohy



## Tenzometre



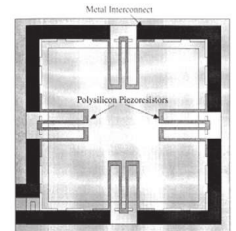
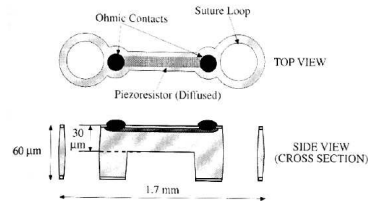
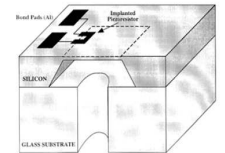
a



Membrane type gauges: typical pressure sensor

## MEMS Tenzometre

Implantable strain gauge



## Využitie tenzometrov Sila

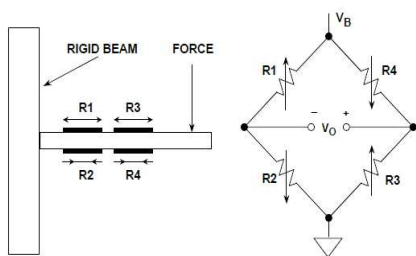


Figure 3.83: A beam force sensor using a strain gage bridge

## Využitie tenzometrov Váženie



### 9.3. Snímače sily Kapacitné snímače

Table 5.1 Fundamental types of capacitive force transducers (CFTs)

Type	Flat Parallel	Cylindrical Coaxial	Spherical Concentric
Layout			
Formula	$C = \frac{\epsilon_r \cdot \epsilon_0 \cdot A}{d}$	$C = \frac{2\pi \epsilon_r \cdot \epsilon_0 \cdot l}{\ln(r_2/r_1)}$	$C = \frac{4\pi \epsilon_r \cdot \epsilon_0 \cdot r_1 \cdot r_2}{r_2 - r_1}$

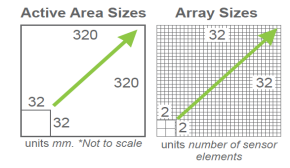
### 9.3. Snímače sily Kapacitné snímače

PPS - TactArray



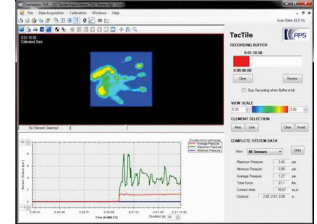
CTAs are flexible and can be molded over complex shapes like a head

#### SENSOR MODELS & METRICS



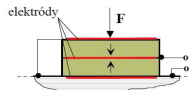
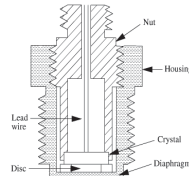
#### Sensor Characteristics & Performance

Full Scale Range	2-80 psi
Thickness	< 1 mm (< 0.04 in)
Signal-to-Noise (SNR)	> 500:1
Minimum Sensitivity	10 Pa (0.0015 psi)
Linearity	99.8%
Gain Non-Repeatability	0.35%
Weight	~ 1.5 lbs (650 g)

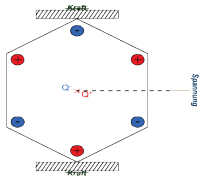
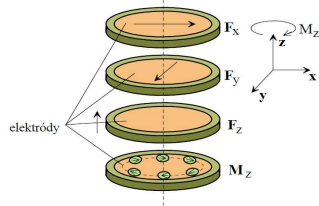


### 9.3. Snímače sily Piezoelektrické snímače

- využívajú vznik náboja pri pôsobení sily ( $U = Q/C$ )
- smer polarizácie - smer citlivosti
- statické merania - náboj po čase "zmlzne"
- materiál - piezokeramika



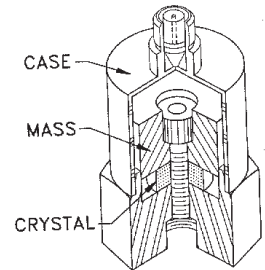
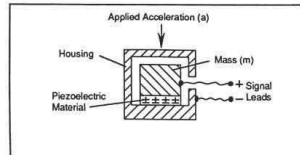
→ vektor polarizácie



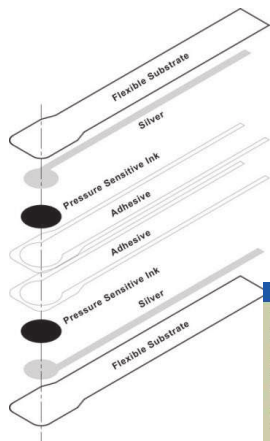
### 9.3. Snímače sily zrýchlenia Piezoelektrické snímače

- teliesko so známou hmotnosťou  $m$ , pri pôsobení sily  $F = m \cdot a$  → snímač zrýchlenia

- meranie vibrácií, diagnostika, monitoring

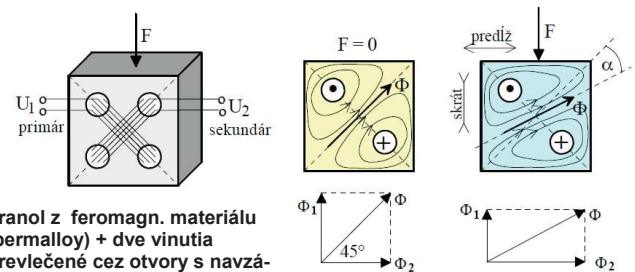


### 9.3. Snímače sily Piezoelektrické snímače



Typical Performance	
Linearity (Error)	< ±3%
Repeatability	< ± 2.5% of Full Scale
Hysteresis	< 4.5% of Full Scale
Drift	< 5% per Logarithmic Time Scale
Response Time	< 5µsec
Operating Temperature	15°F - 140°F (-9°C - 60°C)

### 9.3. Snímače sily Magnetoanizotropné snímače



hranlo z feromagn. materiálu (permalloy) + dve vinutia prevlečené cez otvory s navzájom ⊥ osami, tvoria transformátor

bez pôsobenia sily sekundár neviaže žiadny mag. tok, U2 je nulové

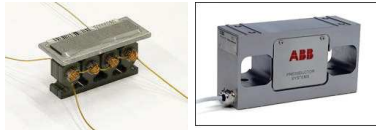
pri silovej deformácii nastanú tieto javy (obecne):  
 ťah → +σ (predĺženie) → μr stúpa → mag tok Φ stúpa  
 tlak → -σ (skrátene) → μr klesá → mag tok Φ klesá



## 9.3. Snímače sily Magnetoanizotropné snímače

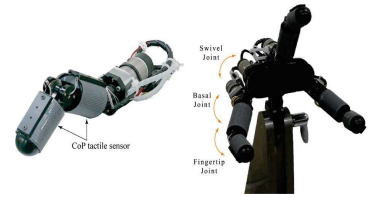
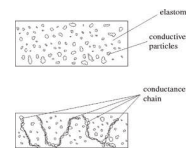
snímač pre  $F = 5000 \text{ kN}$   
(fy ASEA Švédsko)

- linearita, presnosť 0,5 %
- hysteréza 0,2 %
- stlačenie 0,05 mm
- preťaženie 200 %
- rozsah teplôt  $+20 \div +80 \text{ }^\circ\text{C}$
- napájacia f 50, 60, 400 Hz



## 9.3. Snímače sily Zmena elektrického odporu

- vodivá guma
- plastické hmoty (polyuretán)



Materiály vykazujú zmenu odporu pri stlačaní  
Miera stlačenia úmerná sile (niekedy pomocná pružina)

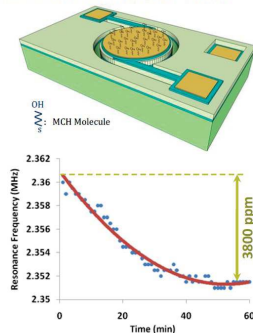
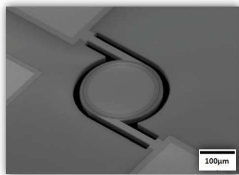
Poznámka: Materiály majú značnú časovú a teplotnú chybu



### 9.3.2 Rezonančné snímače sily Detekcia DNA

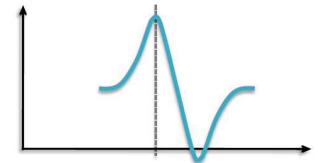
#### Piezoelectric Disk Resonators for Direct Molecular Sensing

- Rotational mode disk resonators are demonstrated as direct real-time bio-molecule monitors
- Exposure to 1.0 mM MCH in aqueous solution
- Saturation is reached after 1hr



## Experiments and Results

### DNA Detection Mechanism

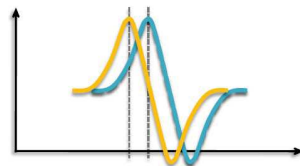
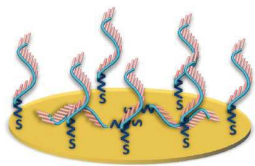


Blank gold surface

- (I) Treatment with HS-ssDNA ( $2.0 \mu\text{M}/1.0 \text{ M KH}_2\text{PO}_4$ , PH 4.2)
- (II) Exposure to 1.0 mM Mercapto-Hexanol in aqueous solution
- (III) Hybridization with Complementary DNA Solution ( $1.0 \mu\text{M}/1.0 \text{ M NaCl Tris-HCl}$  1.0 mM EDTA)

## Experiments and Results

### DNA Detection Mechanism

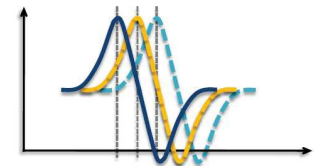
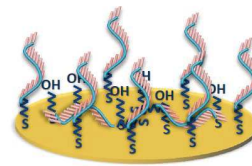


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## Experiments and Results

### DNA Detection Mechanism



Blank gold surface

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## 9.4. Snímače zrýchlenia

$$a = \lim_{\Delta t \rightarrow 0} \frac{\Delta v}{\Delta t} = \frac{dv}{dt}$$

SI jednotka je **m/s<sup>2</sup>**

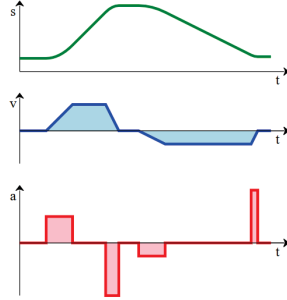
$$F = m \cdot a$$

$$F = k \cdot \Delta x$$

$$a = \frac{k}{m} \Delta x$$

$$a_g = \frac{M}{R^2}$$

9,764 – 9,834 m/s<sup>2</sup>

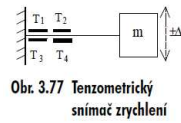


Zdola nahor:  
časový priebeh zrýchlenia  $a(t)$ ,  
integrál zrýchlenia je rýchlosť  $v(t)$ ,  
a integrovaním rýchlosti získame  
priebeh dráhy  $s(t)$ .

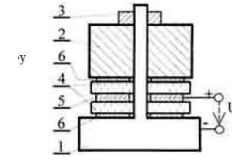
## 9.4. Snímače zrýchlenia

- Zrýchlenie  $a = dv / dt$
- Newtonov zákon  $F = m \cdot a$

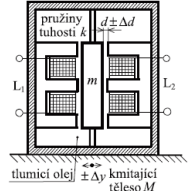
Pri známej hmotnosti telesa  $m$  je sila  $F$  merítkom zrýchlenia  $a$ .



Obr. 3.77 Tenzometrický snímač zrýchlenia

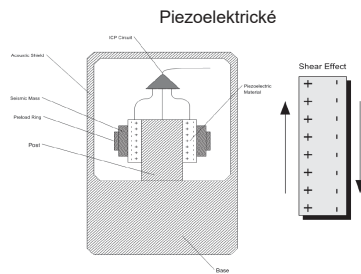
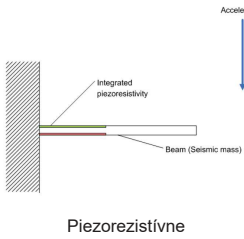


Obr. 3.78b Piezoelektrický tlakový snímač zrýchlenia



Obr. 3.79 Indukčný snímač zrýchlenia

## 9.4. Snímače zrýchlenia – akcelerometre



## 9.4. Meranie zrýchlenia

### Applications of MEMS Accelerometers



- Industrial**
- Platform stabilization
  - Oil drilling orientation
  - Robotic telepresence



- Automotive**
- Airbag deployment
  - Rollover, anti-skid control



- Consumer**
- Interactive gaming
  - Free-fall detection
  - Camera stabilization
  - Indoor navigation

- Military**
- Aircraft flight control
  - Dead-reckoning



Georgia Tech

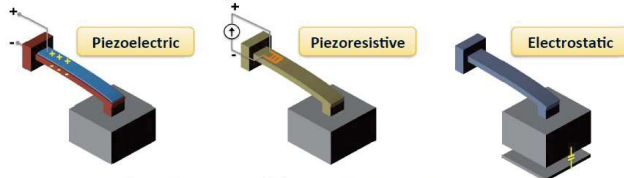
Qualtré

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## 9.4. Meranie zrýchlenia

### Electromechanical Transduction

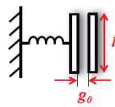
- Displacement has to be converted into electrical signal
- Most common sensing mechanisms:



- Most popular: electrostatic (capacitive) sensing

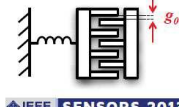
**Parallel Plate**

$$\frac{dC}{dx} = \frac{\epsilon \cdot W \cdot t}{(g_0 - x)^2}$$



**Comb Structure**

$$\frac{dC}{dx} = \frac{\epsilon \cdot 2n \cdot t}{g_0}$$



$t$ : thickness,  $n$ : # of fingers

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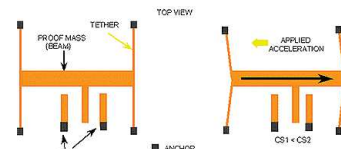
## 9.4. Meranie zrýchlenia

### MEMS akcelerometer

#### ADX1202: ±2 g Dual Axis Accelerometer

##### Features

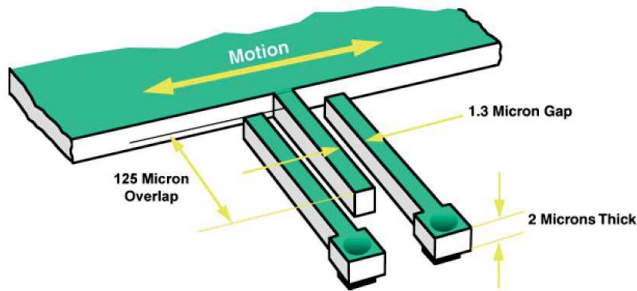
- X and Y Axis on a single chip = Small size and lower cost
- 250uA per Axis = Low power battery operation
- 3.0V to 5.0V Operation = Low power battery operation
- Surface mount package = Small size and ease of use
- High resolution PWM converter = Direct interface to micro (No A/D)
- iMEMS = Low cost AND high performance



SENSOR AT REST

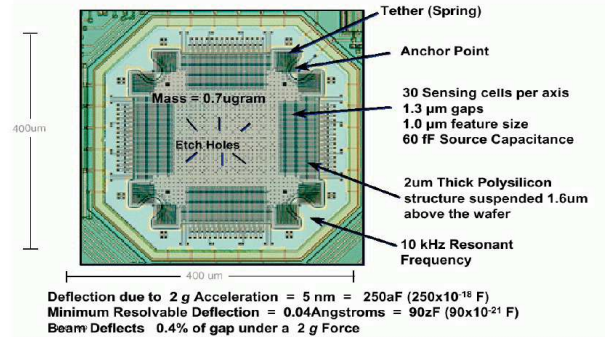
RESPONDING TO AN APPLIED ACCELERATION (MOVEMENT SHOWN IS GREATLY EXAGGERATED)

## 9. 4. Meranie zrýchlenia MEMS akcelerometer



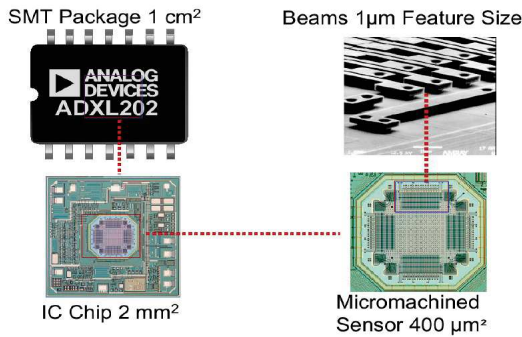
## 9. 4. Meranie zrýchlenia MEMS akcelerometer

ADXL 202: Micromachined Beam

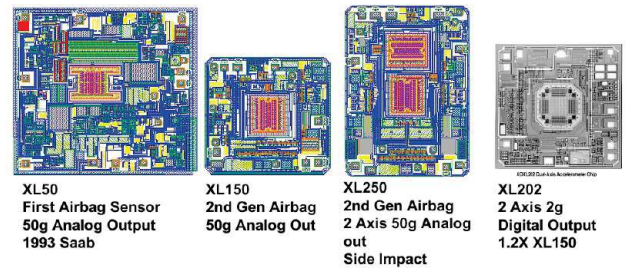


## 9. 4. Meranie zrýchlenia MEMS akcelerometer

ADXL 202: acceleration sensor



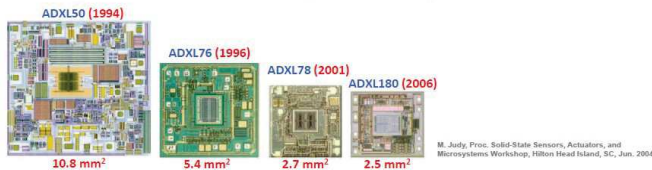
## 9. 4. Meranie zrýchlenia MEMS akcelerometer



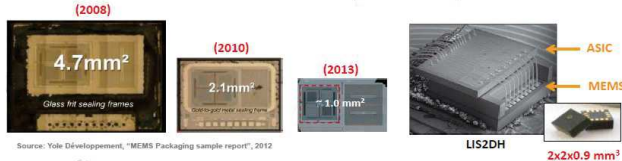
## 9. 4. Meranie zrýchlenia Evolution of MEMS Accelerometers

3

- Analog Devices Accelerometer (Automotive)



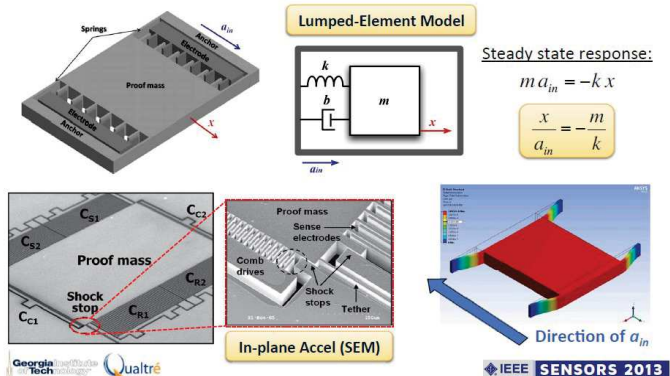
- STMicroelectronics Accelerometer (Consumer)



## 9. 4. Meranie zrýchlenia MEMS Capacitive Accelerometers

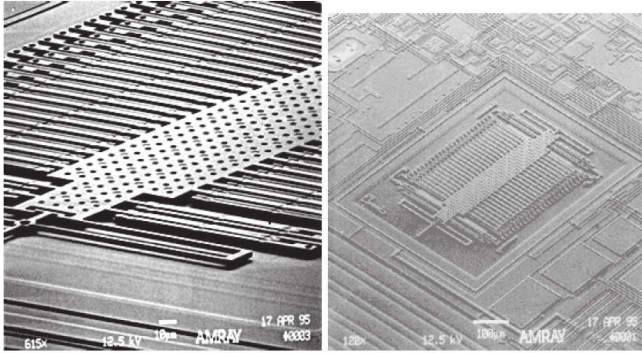
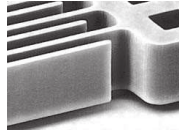
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- Conventional MEMS accelerometer architecture

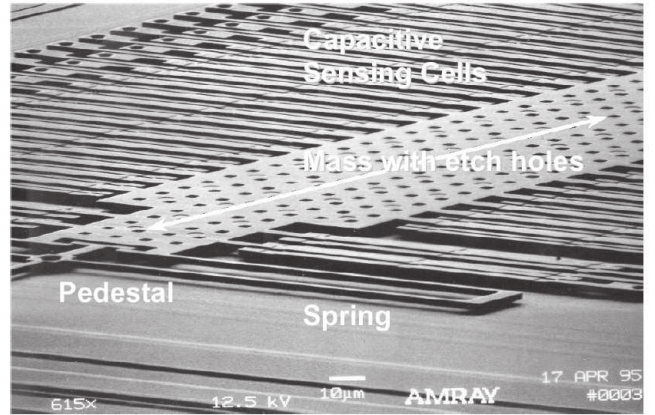




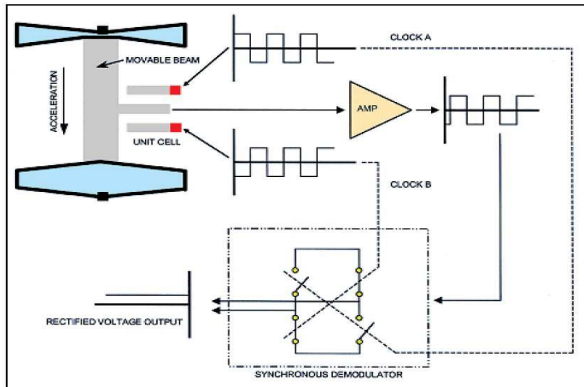
### 9. 4. Meranie zrýchlenia MEMS akcelerometer



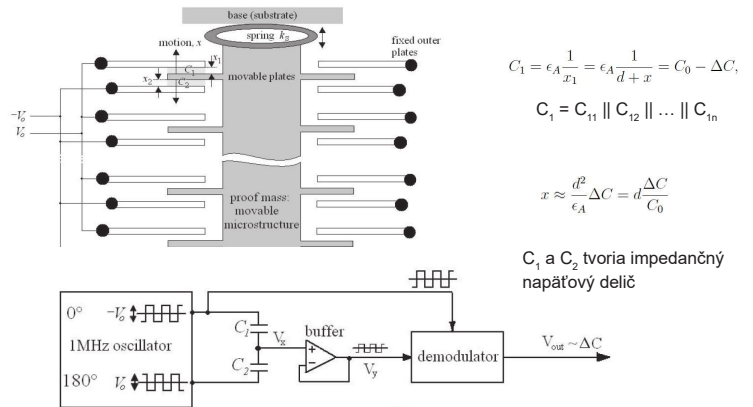
### 9. 4. Meranie zrýchlenia MEMS akcelerometer



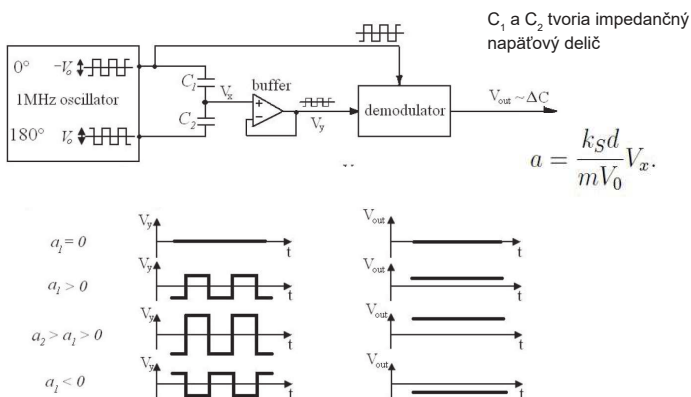
### 9. 4. Meranie zrýchlenia MEMS akcelerometer



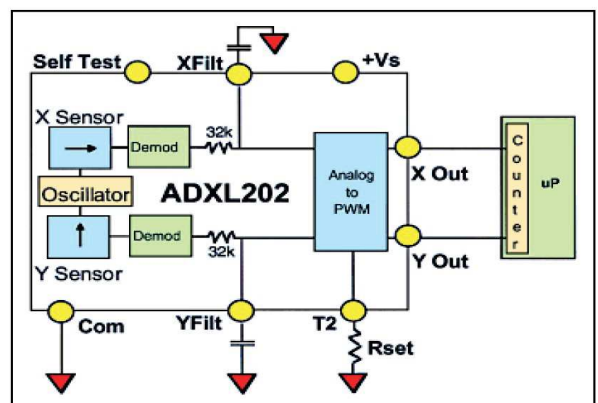
### 9. 4. Meranie zrýchlenia MEMS akcelerometer



### 9. 4. Meranie zrýchlenia MEMS akcelerometer

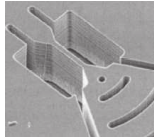
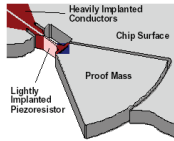


### 9. 4. Meranie zrýchlenia MEMS akcelerometer



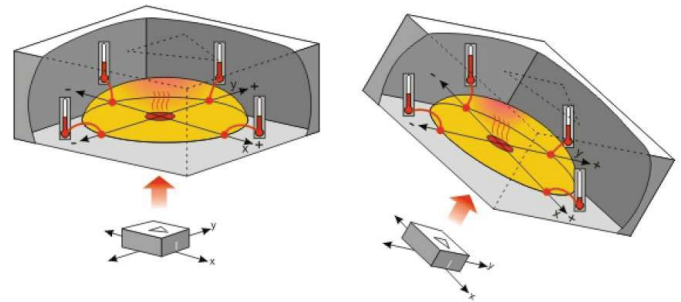
## 9. 4. Meranie zrýchlenia MEMS akcelerometer

- Piezoresistive MEMS accelerometer
  - Operating Principle: a proof mass attached to a silicon housing through a short flexural element. The implantation of a piezoresistive material on the upper surface of the flexural element. The strain experienced by a piezoresistive material causes a position change of its internal atoms, resulting in the change of its electrical resistance
  - low-noise property at high frequencies

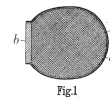


Courtesy of JP Lynch, U Mich.

## 9. 4. Meranie zrýchlenia MEMS MX2125 hot bubble



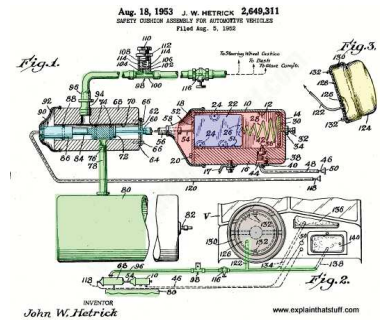
A. H. PARROTT AND H. ROUND,  
AIR CUSHION.  
APPLICATION FILED NOV. 21, 1911.  
1,381,359. Patented Feb. 17, 1920.



United States patent submitted in 1919 by two dentists, **Harold Round & Arthur Parrott** of Birmingham, England

**John Hetrick's** original airbag design from 1953

**Allen K. Breed** (1927–2000), who developed a variety of different ways of triggering the explosion of gas inside an airbag just before the impact of a crash.

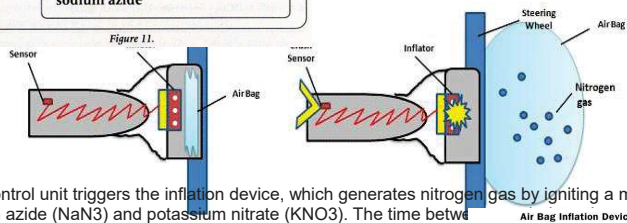


Bellis, Mary. "The History of Airbags." ThoughtCo, Feb. 11, 2020, thoughtco.com/history-of-airbags-1991232.

**AUTOMOBILE AIRBAG**  
AIRBAG VOLUME: 2.3 cubic feet  
AIRBAG FILLING TIME: 0.030 seconds

**Chemical Reaction:**  
 $2 \text{NaN}_3 \rightarrow 2 \text{Na} + 3 \text{N}_2 \text{ (gas)}$   
sodium azide

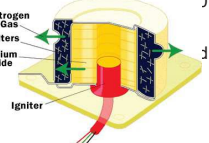
Gas Generator Reaction	Reactants	Products
First Reaction (Triggered by Sensor)	$\text{NaN}_3$	$\text{Na}$ $\text{N}_2 \text{ (g)}$
Second Reaction	$\text{Na}$ $\text{KNO}_3$	$\text{K}_2\text{O}$ $\text{Na}_2\text{O}$ $\text{N}_2 \text{ (g)}$
Final Reaction	$\text{K}_2\text{O}$ $\text{Na}_2\text{O}$ $\text{SiO}_2$	alkaline silicate (glass)



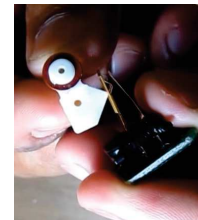
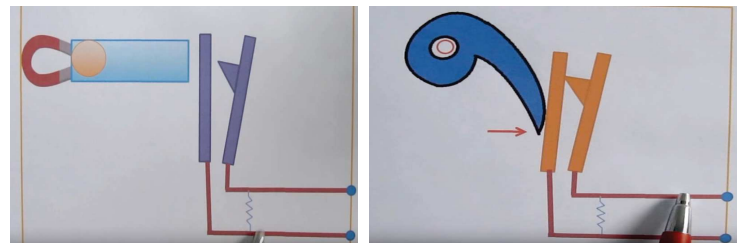
This control unit triggers the inflation device, which generates nitrogen gas by igniting a mixture of sodium azide ( $\text{NaN}_3$ ) and potassium nitrate ( $\text{KNO}_3$ ). The time between complete deployment of the airbag is approximately 0.05 seconds. T mph, which itself can be harmful in certain cases.

Most systems use a weight sensor in the front passenger seat to determine if it is not, the passenger airbag will not deploy. The weight sensor is designed to detect children and adults who may be occupying the seat.

[https://cecas.clemson.edu/cvel/auto/systems/airbag\\_deployment.html](https://cecas.clemson.edu/cvel/auto/systems/airbag_deployment.html)  
<http://allaboutairbagdeployment.weebly.com/part-three.html>



## Mechanické





# Mechanické

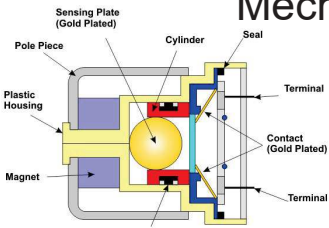


Figure 1. Structural components to an Inertia sensor. Source: Duffy, J.E. (2001). I-Car Professional Automotive Collision Repair. New York: Delmar, a division of Thomas Learning.

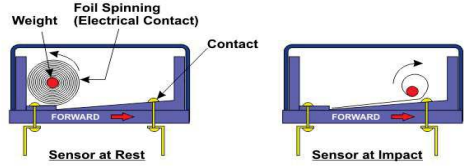
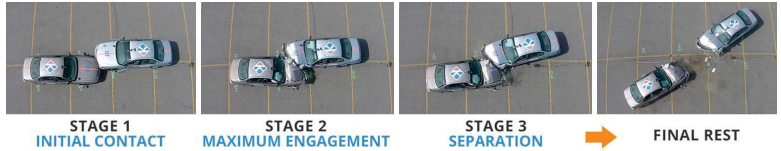
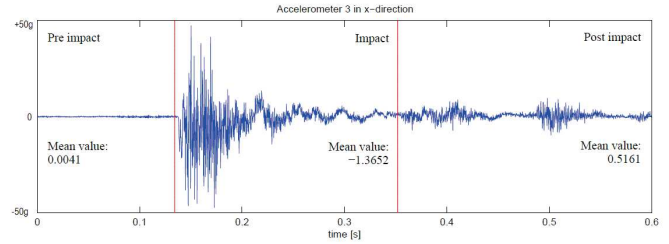


Figure 2. Functional principle to a typical roller type airbag sensor. Source: Erjavec, J. (2010). Automotive Technology: A Systems Approach. New York: Delmar, Cengage Learning.

<https://www.azosensors.com/article.aspx?ArticleID=40>



the airbag deployment decision depends upon acceleration and jerk



## Airbagy – deploy or not deploy?

### Longitudinal Speed, Acceleration & Jerk

Offset Head-on Crash Test - Bullet Vehicle (2016 Crash Test #2)

