

# Where am I?



Senzory pre navigáciu a orientáciu

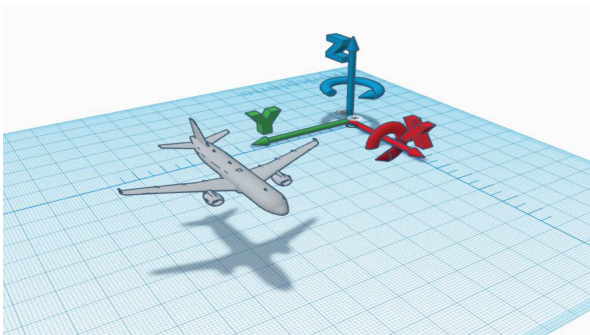
## Súradnicové systémy

**Kartézsky súradnicový systém**  
René Descartes (Cartesius)  
31. 3. 1596 – 11. 2. 1650  
Francúzsky filozof, matematik a vedec.

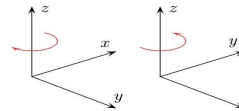


**Lat/Lon systém**  
**Valcové súradnice**  
**Sférické súradnice**

## Súradnicové systémy: Kartézsky systém

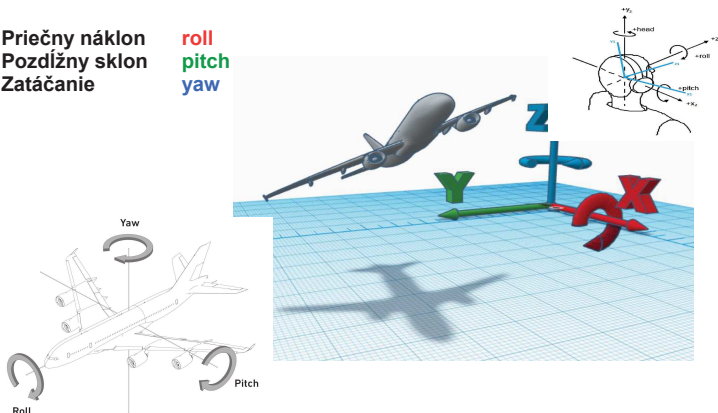


## Right hand rule

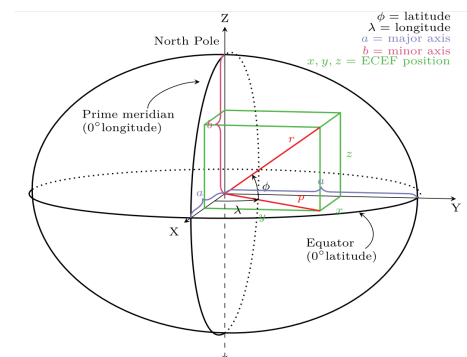


[https://www.snb.ch/en/f/about/cash/series9/design\\_series9/ld/cash\\_series9\\_design\\_200](https://www.snb.ch/en/f/about/cash/series9/design_series9/ld/cash_series9_design_200)

Priečny náklon **roll**  
Pozdĺžny sklon **pitch**  
Zatáčanie **yaw**

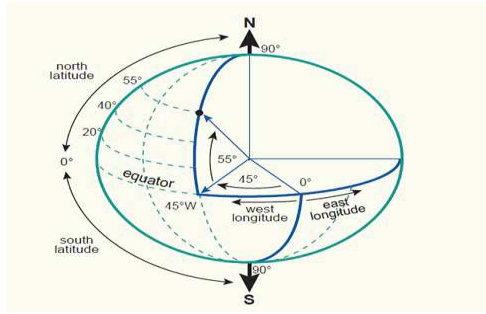


## Súradnicové systémy



$\phi$  = latitude  
 $\lambda$  = longitude  
 $a$  = major axis  
 $b$  = minor axis  
 $x, y, z$  = ECEF position

# Súradnicové systémy



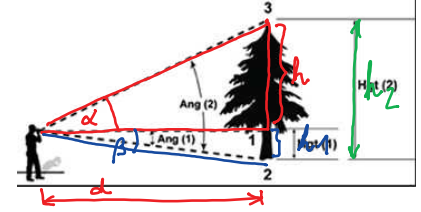
# Triangulácia

$$h = d \cdot \operatorname{tg} \alpha$$

$$h_1 = d \cdot \operatorname{tg} \beta$$

(akho odhad výšky postavy 1,8 m)

$$h_2 = h + h_1$$

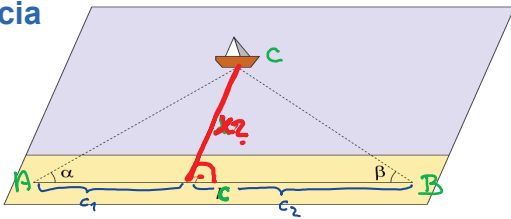


# Triangulácia

$$c = c_1 + c_2$$

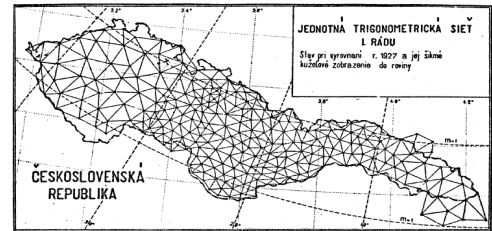
$$\operatorname{tg} \alpha = \frac{x}{c_1}$$

$$\operatorname{tg} \beta = \frac{x}{c_2}$$



$$x = c \cdot \frac{\operatorname{tg} \alpha \cdot \operatorname{tg} \beta}{\operatorname{tg} \alpha + \operatorname{tg} \beta}$$

# Triangulácia

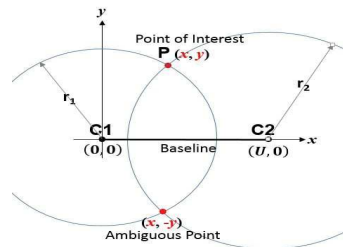


Obr.1.1 Jednotná trigonometrická sieť I. rádu reprezentujúca pôvodnú realizáciu JTSK, prevzaté z (Abelovič, 1990).

# Triangulácia



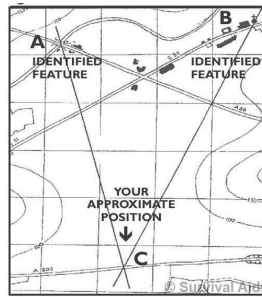
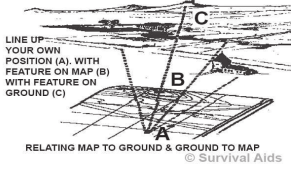
# Trilaterácia



$$x = \frac{r_1^2 - r_2^2 + U^2}{2U}$$

$$y = \pm \sqrt{r_1^2 - x^2}$$

## Navigácia: Kde som?



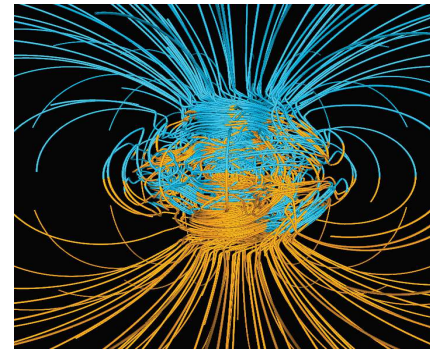
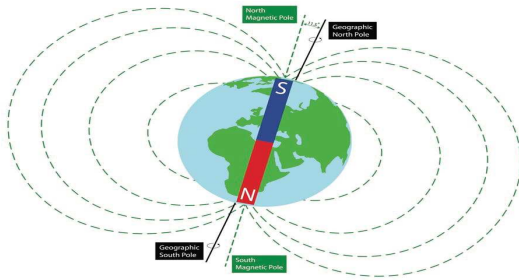
## História: mapa + kompas



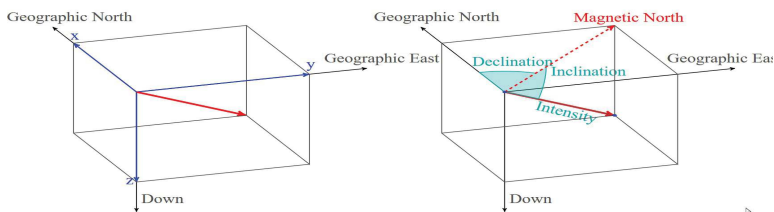
Model of a Han Dynasty (206 BC–220 AD) south-indicating ladle or sinan. It is theorized[by whom?] that the south-pointing spoons of the Han dynasty were magnetized lodestones.[28]

## Senzory magnetického poľa - kompas

### The Earth's Magnetic Field



[https://en.wikipedia.org/wiki/Earth%27s\\_magnetic\\_field#/media/File:Geodynamo\\_Between\\_Reversals.gif](https://en.wikipedia.org/wiki/Earth%27s_magnetic_field#/media/File:Geodynamo_Between_Reversals.gif)

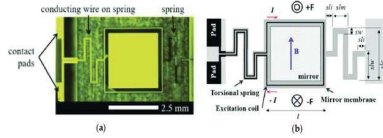
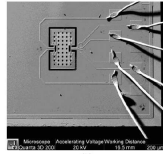
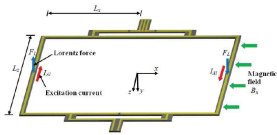
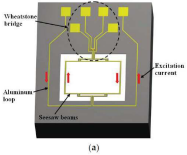
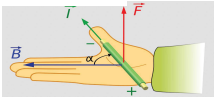


## Magnetometer

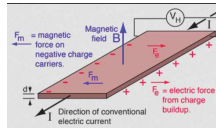
- AMR magnetometer
- GMR magnetometer
- Hall-Effect sensor
- Lorentz force-based MEMS sensor
- MEMS compass, and
- magnetic-field sensor

## Lorentzova sila

$$\mathbf{F} = I \mathbf{l} \times \mathbf{B}$$



## Hallov jav

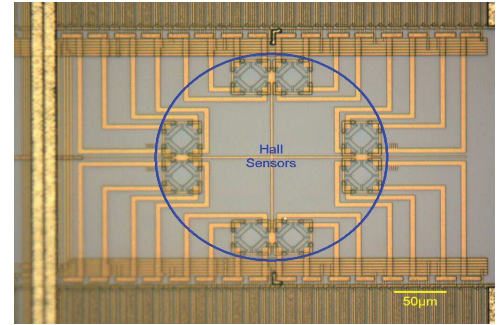


$$V_H = \frac{I_x B_z}{nte}$$

Vychýlenie elektrónov spôsobuje Lorentzova sila

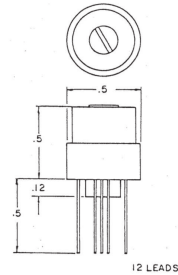
<https://www.memsjournal.com/2011/02/motion-sensing-in-the-iphone-4-electronic-compass.html>

AK8973 Hall sensor layout.



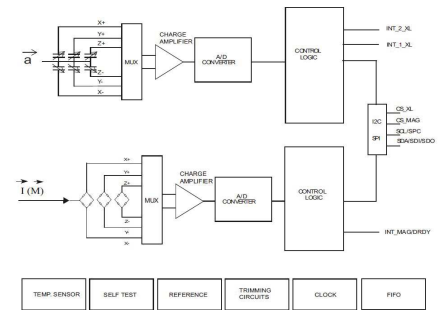
## Dinsmore 1490

- miniature permanent magnet rotor
- jewel suspension + 4x Hall sensor
- response time 3.5 second (intentionally)
- weight 2.25 g
- temperature -20 – +85 deg C
- Vcc = 5 to 20 V



## LSM303AGR

- 3 magnetic field channels
- 3 acceleration channels
- ±50 gauss magnetic dynamic range
- ±2/±4/±8/±16 g selectable acceleration full scales
- 16-bit data output
- SPI / I2C serial interfaces
- Analog supply 1.71 V to 3.6 V
- Internal temperature sensor
- Self test procedures



## Dead reckoning

počítanie mŕtvych  
– navigácia výpočtom

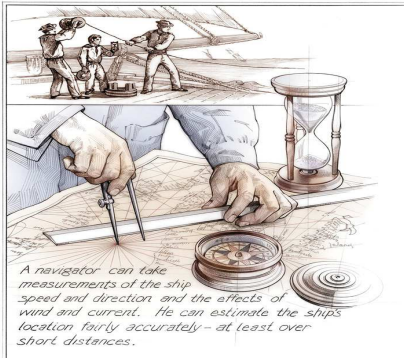
Polohu odvodíme od predošlých polôh na základe známeho smeru a rýchlosti

### Odometria

– jedna z metód, používa sa odvažovanie kolesa, alebo IRC snímač

### Inerciálna jednotka

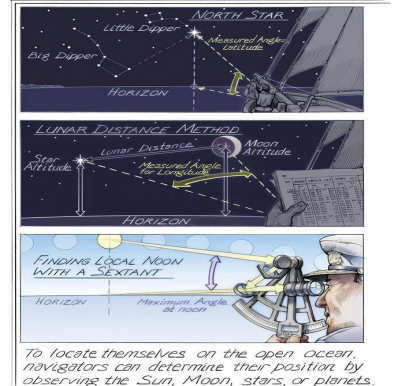
### DEAD RECKONING AT SEA



## Navigácia na mori

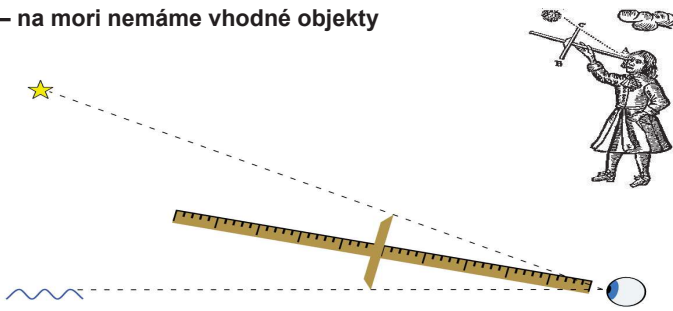
– na mori ani vo vzduchu nemáme vhodné referenčné objekty

### CELESTIAL NAVIGATION AT SEA



## Hviezdna navigácia – Jakubova tyč

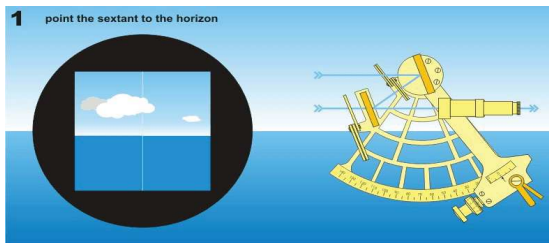
– na mori nemáme vhodné objekty



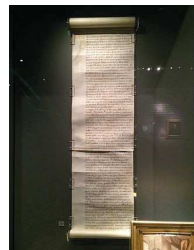
## Hviezdna navigácia – sextant



## Hviezdna navigácia – sextant



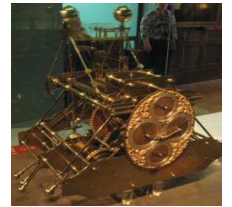
## Zemepisná dĺžka – hodiny



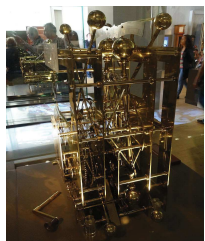
The Longitude Act 1714



John Harrison



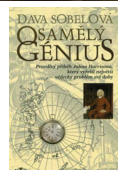
Chronometer H1



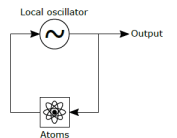
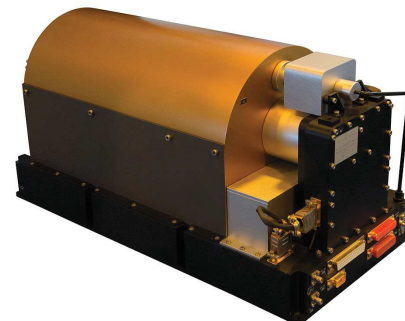
Chronometer H2



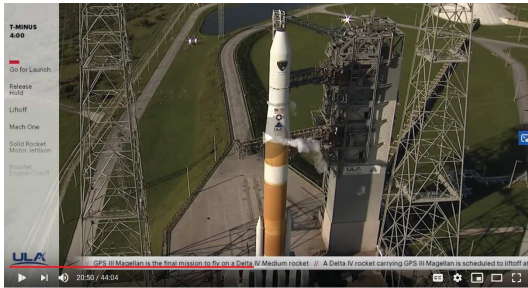
Chronometer H4



## Atómové hodiny



## Introduction video

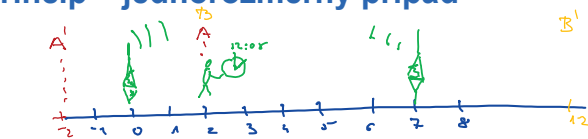


<https://youtu.be/0AgjyDoXtE?t=1539>

## Global Navigation Satellite System

### GNSS

## Princíp – jednorozmerný prípad



- a) jeden vpratač: Na hodinkách vidím 12:01  
 a počujem: „Som vpratač 6 a je 12:03“  
 ⇒ Som 2m od bodu 'd' ⇒ A, resp. A'
- b) dve vpratače: Na hodinkách vidím 12:05  
 a počujem: „Som vpratač 6 a je 12:03“  
 a „Som vpratač 7 a je 12:00“  
 ⇒ pribudne body B a B' ⇒ prácha je A∩B

## Čo ak nemáme presné hodinky na ruke?

Pozívam: Som 6 a je 12:03  
 Som 7 a je 12:00

Je čas 12:06? neznáme.  
 ak vieme, že: '6' a '7' sú vzdialené 7-0=7

$$\text{Takže } \underbrace{(t-3)}_{\text{od '6'}} + \underbrace{(t-0)}_{\text{od '7'}} = 7$$

$$t-3+t-0=7$$

$$2t=10$$

$$t=5$$

⇒ je čas 12:05  
 a viem koľko je hodín

## Princíp v rovine – priamka, rovina

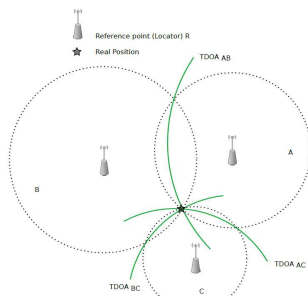


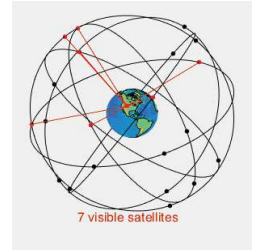
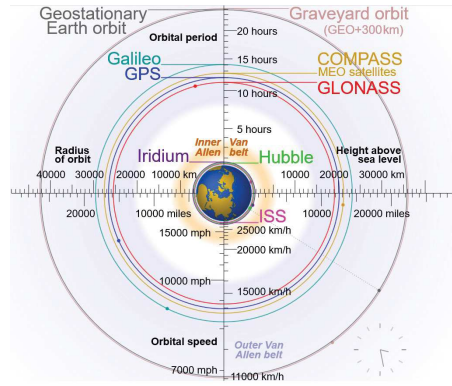
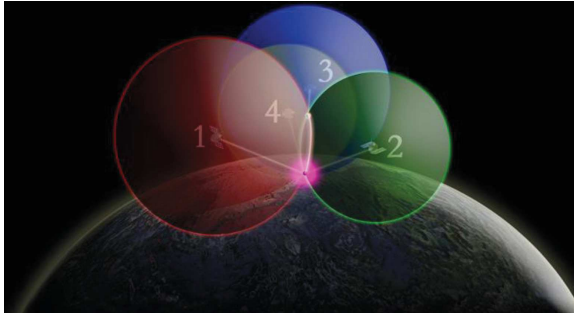
Figure 6. Time difference of arrival (TDOA)-based algorithms.

Káždé meranie je  
 zatiaľ čo nepresnosť:  
 nepresnosť každého vpratača  
 toto môže byť  
 správnou polhou

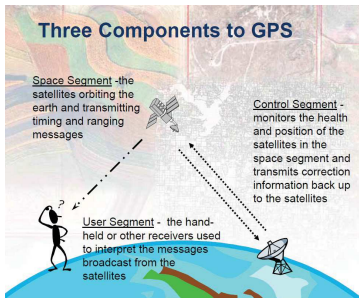
## V priestore



## V priestore



## Tri segmenty GPS



## GPS = hodiny

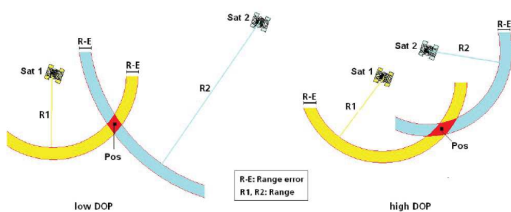
### The Clock Problem



- To measure distance from speed of light we need a VERY accurate clock (clock error of 1/100 sec = distance error of 3000 km!).
- GPS Satellites have very accurate atomic clocks.
- Our receivers do not have atomic clocks, so how can we measure time with necessary accuracy?

## Satellite Geometry

### Presnost'

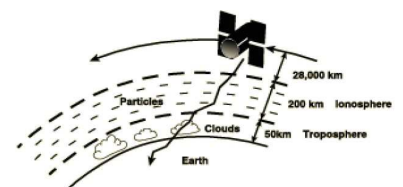


## Atmospheric Effect

### Presnost'

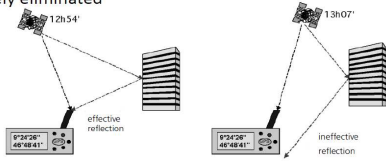
- GPS signal slowed down through the charged particles of the **ionosphere** and then through the water vapor in the **troposphere**

- Must correct for atmospheric effects with modeling



## Multi-Path

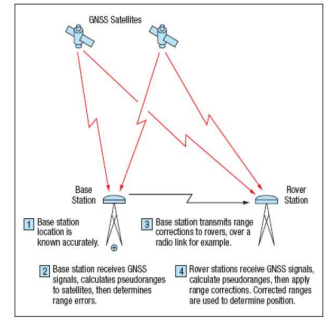
- Signals can be reflected on the way to the receiver. This is called “multipath propagation”
- These reflected signals are delayed from the direct signal, and if strong enough, can interfere with the direct signal
- Techniques have been developed whereby the receiver only considers the earliest-arriving signals and ignore multipath signals, which arrives later
- It cannot be entirely eliminated



## Presnost'

## Differential GPS (DGPS)

- Differential GNSS uses a fixed GNSS receiver, referred to as “base station” to transmit corrections to the rover station for improved positioning
- Error due to signal transmission through the atmosphere can be corrected using DGPS
- Atmospheric errors are the same over short distances.
- Error in base station, can be removed from remote (roving) receiver position, and code phase signal.



## NMEA 0183

### National Marine Electronics Association standard

combined **electrical** and **data** specification for communication between *marine electronics* echo sounder, sonars, anemometer, gyrocompass, autopilot, GPS receivers,...

**electrical** EIA-422 (most hardware also EIA-232),  
typ. Baud rate 4800, 8 data, none parity, 1 stop, no handshake

**data** – simple ASCII, serial protocol, data are transmitted in a "sentence"

**\$XYYYY, a1, a2, a3, . . . ., an\*cc<CR><LF>**

- XX: **GP** – GPS, **GL** – GLONASS, **GA** - Galileo  
 YYY: **RMC** - recommended minimum data - základné údaje, ktoré poskytujú všetky prijímače  
**GGA** - sada údajov o odchýlkach pre presnejšiu lokalizáciu  
**GSA** - zoznam čísel max. 12 satelitov, použitých pre navigáciu  
**GSV** – podrobnejšie údaje o satelitoch - sila signálu a poloha na oblohe  
**GLL** - Lat/Lon - len geografická poloha a čas (podmnožina údajov RMC)

## NMEA 0183

### RMC veta

\$GPRMC, 161229.487,A,3723.2475,N,12158.3416,W,0.13,309.62,120598, #10

Table 1-11 RMC Data Format

Name	Example	Units	Description
Message ID	\$GPRMC		RMC protocol header
UTC Time	161229.487		hhmmss.sss
Status <sup>1</sup>	A		A=data valid or V=data not valid
Latitude	3723.2475		ddmm.mmmmm
N/S Indicator	N		N=north or S=south
Longitude	12158.3416		dddmm.mmmmm
E/W Indicator	W		E=east or W=west
Speed Over Ground	0.13	knots	
Course Over Ground	309.62	degrees	True
Date	120598		ddmmyy
Magnetic Variation <sup>2</sup>		degrees	E=east or W=west
Mode	A		A=Autonomous, D=DGPS, E=DR
Checksum	#10		
<CR> <LF>			End of message termination

1. A valid status is derived from the SIRF Binary MLD 2 position mode 1. See the *SIRF Binary Protocol Reference Manual*.  
 2. SIRF Technology Inc. does not support magnetic declination. All "course over ground" data are geodetic WGS84 directions.

## NMEA 0183

### GLL veta

\$GPGLL, 3723.2475,N,12158.3416,W,161229.487,A,A\*41

Table 1-5 GLL Data Format

Name	Example	Units	Description
Message ID	\$GPGLL		GLL protocol header
Latitude	3723.2475		ddmm.mmmmm
N/S Indicator	N		N=north or S=south
Longitude	12158.3416		dddmm.mmmmm
E/W Indicator	W		E=east or W=west
UTC Time	161229.487		hhmmss.sss
Status	A		A=data valid or V=data not valid
Mode	A		A=Autonomous, D=DGPS, E=DR (Only present in NMEA version 3.00)
Checksum	#41		
<CR> <LF>			End of message termination

## Copernicus II (12 Channel)

Size : 19x19x2.54mm  
 Sensitivity : -160dBm  
 Time to First Lock (cold start) : 38 sec  
 Dual serial ports with reconfigurable UART rates  
 NMEA, TSIP, and TAIP protocols



Update rate	Update rate
TSIP 1 Hz	TSIP 1 Hz
NMEA 1 Hz	NMEA 1 Hz
TAIP 1 Hz	TAIP 1 Hz
<b>Accuracy (24 hour static)</b>	<b>Accuracy (24 hour static)</b>
Horizontal (without SBAS) <2.5 m 50%, <5 m 90%	Horizontal (without SBAS) <2.5 m 50%, <5 m 90%
Horizontal (with SBAS) <2.0 m 50%, <4 m 90%	Horizontal (with SBAS) <2.0 m 50%, <4 m 90%
Altitude (without SBAS) <5 m 50%, <8 m 90%	Altitude (without SBAS) <5 m 50%, <8 m 90%
Altitude (with SBAS) <3 m 50%, <5 m 90%	Altitude (with SBAS) <3 m 50%, <5 m 90%
Velocity 0.06 m/sec	Velocity 0.06 m/sec
PPS (static) ±60 ns RMS	PPS (static) ±60 ns RMS
PPS (stationary mode indoors at -145 dBm) ±350 ns RMS	PPS (stationary mode indoors at -145 dBm) ±350 ns RMS



# NEO-6

50 Channels	
GPS L1 frequency, C/A Code	
SBAS: WAAS, EGNOS, MSAS	
	NEO-6GQT
Cold Start <sup>1</sup>	26 s
Warm Start <sup>2</sup>	26 s
Hot Start <sup>2</sup>	1 s
Aided Starts <sup>3</sup>	1 s
	NEO-6GQT
Tracking & Navigation	-162 dBm
Reacquisition <sup>4</sup>	-160 dBm
Cold Start (without aiding)	-148 dBm
Hot Start	-157 dBm
	NEO-6GQMT
	5Hz
GPS	2.5 m
SBAS	2.0 m
SBAS + PPP <sup>7</sup>	< 1 m (2D, R50) <sup>8</sup>
SBAS + PPP <sup>7</sup>	< 2 m (3D, R50) <sup>8</sup>

Accuracy: 1.8m  
 Search channels: 66  
 Tracking channels: 22  
 Sensitivity: -165dBm  
 Update rate: 10Hz



# BCM47755

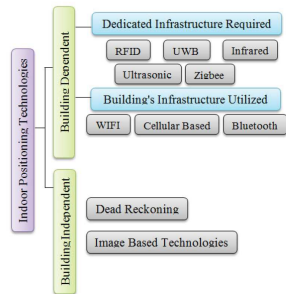
1. ARM-based 32-bit Cortex-M4F
2. ARM-based Cortex-M0

Simultaneously receive the following signals:

- GPS L1 C/A
- GLONASS L1
- BeiDou (BDS) B1
- QZSS L1
- Galileo (GAL) E1
- GPS L5
- Galileo E5a
- QZSS L5



# Indoor navigation



# Real Time Location Systems

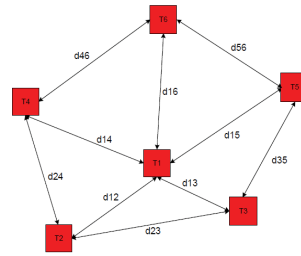


Figure 3: Relative location among a group of nodes

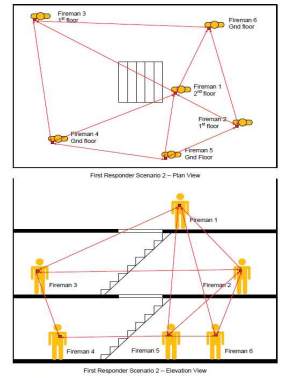


Figure 4: First responder scenario

# Real Time Location Systems

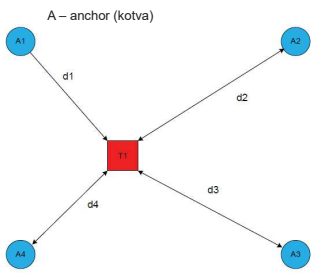


Figure 2: RTLS with fixed infrastructure



Sledovanie a lokalizácia pacientov a materiálu v zdravotníctve



Sledovanie a lokalizácia tovaru a balíkov, paliet v skladoch a logistike.



Sledovanie a monitoring zvierat v živočíšnej výrobe



Sledovanie stavu a pohybu materiálu, zásob, polotovarov v priemyselnej výrobe.

# Real Time Location Systems

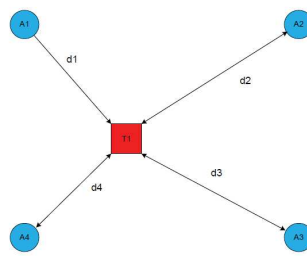


Figure 2: RTLS with fixed infrastructure

### Evaluation:

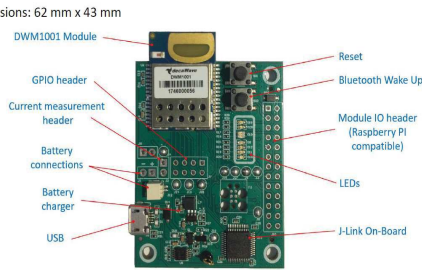
- Received Signal Strength (RSS)
- Time Of Arrival (TOA)
- Time Difference Of Arrival (TDOA)
- Angle of arrival (AOA)

## Ultra Wideband (UWB) transceiver Decawave DW1000



### Key Features

- Ranging accuracy to within 10cm
- UWB Channel 5 PCB antenna (6.5 GHz)
- 6.8 Mbps data rate
- 60 m line-of-sight range typical
- IEEE802.15.4-2011 UWB compliant
- Nordic Semiconductor nRF52832
- Bluetooth connectivity with antenna
- Motion sensor: 3-axis accelerometer
- Current consumption sleep mode: <math><15\mu A</math>
- Supply voltage: 2.8 V to 3.6 V
- Size: 19.1 mm x 26.2 mm x 2.6 mm



## Ultra Wideband (UWB) transceiver Decawave DW1000

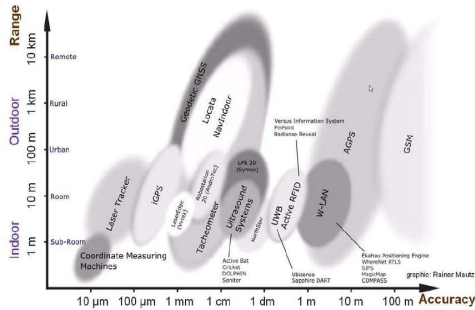
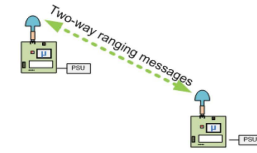
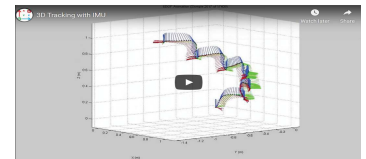


Figure 2.1: Overview of infrastructure-based indoor positioning methods and according accuracies as presented by Mautz (2009)

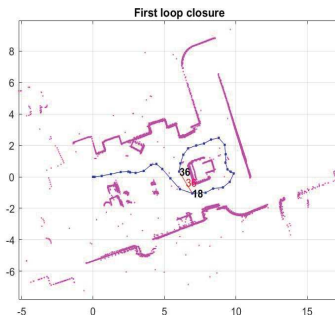
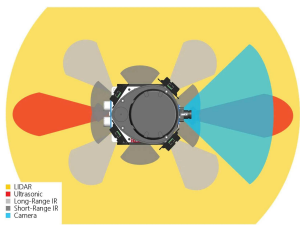
## Lokalizácia a navigácia s mapou prostredia Inertial Measurement Unit (IMU)

<https://www.youtube.com/watch?v=TJIntyaSNqM>

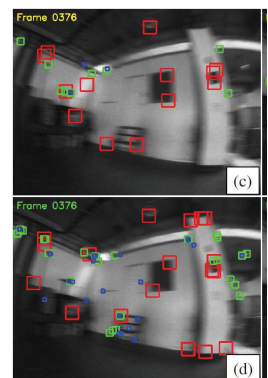
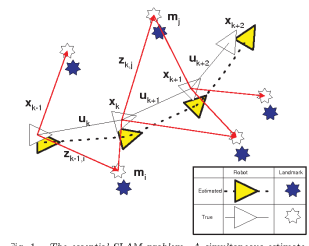


<https://x-io.co.uk/gait-tracking-with-x-imu/>

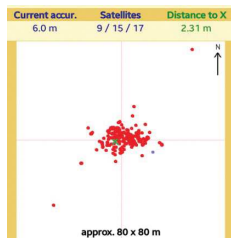
## 10. Lokalizácia a navigácia bez mapy Simultaneous Localization and Mapping (SLAM)



## 10. Lokalizácia a navigácia Visual SLAM

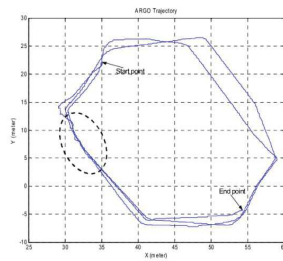


## Cvičenia



approx. 80 x 80 m

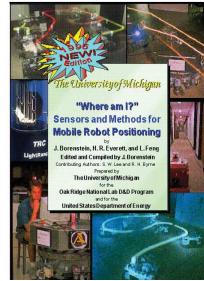
6 hodín merania



3x: polygón 1 km peši  
4 km autom

[http://senzor.robotika.sk/sensorwiki/index.php/Meranie\\_s\\_GPS](http://senzor.robotika.sk/sensorwiki/index.php/Meranie_s_GPS)

## Chcem vedieť viac...



<http://www-personal.umich.edu/~johannb/Papers/pos96rep.pdf>

